

# Neural Decompositional Memory

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## 1 Motivations

- Recent trends in learning to decompose, disentangle, explainable AI
- Memory role in representing concept hierarchy or decomposition is not clear
- This paper aims to give another way to explain the role of memory in this problem

## 2 Latent Encoder Decoder Framework with External Memory

- VMED learns a MoG of the prior distribution for latent space, which is a form of decomposition.
  - However, its writing/reading mechanisms are DNC-like and not supportive for decompositional functionalities.
  - The KL divergence between MoG and Gaussian is only estimation and hard to optimize
  - There is no constraint on the component of the priors, which reduces decompositional functionalities
- The idea in VMED that each memory slot stores a component of the latent space is simple yet fundamental. If we assume the idea is correct, we can view there is an inner latent encoding-decoding process:  $z \rightarrow \mathbf{M} \rightarrow z'$ , where the memory  $\mathbf{M}$  stores the components (bases) of the latent space
  - Latent Encoding: Decompose (project) the latent vector into memory slots
  - Latent Decoding: Compose (reconstruct) the latent vector from the bases stored in  $\mathbf{M}$

### 3 Latent Encoding - Memory Writing: Recurrent projections with Stored-Program Memory

- At each step of latent encoding, we need to generate a network  $W_t$  to project  $z \rightarrow m_t : m_t = W_t z$ . The memory is composed by  $\{m_t\}_{t=1}^N$  row-wise.
- We can use any weight generator, including NSM:  $W_t = NSM([z, h_t])$  where  $h_t$  is the hidden state of some RNN to make the system recurrent.
- Using NSM means we assume there are few main projectors that can be interpolated to decompose the latent data to its bases

### 4 Latent Decoding - Memory Reading: Least-square Attention

- Given  $\mathbf{M}$ , we want to reconstruct the latent vector by reading from the memory. The reading weight is the solution to the least square problem:

$$w_t = \underset{w}{\operatorname{arg\,min}} \|z - \mathbf{M}^\top w\|$$

- Basically, we want to attend to memory slots that compose the best linear estimator of  $z$ . The solution has a known form:  $w_t = (\mathbf{M}\mathbf{M}^\top)^{-1} \mathbf{M}z$
- Again, we may want to make it recurrent, we read multiple times before determining the final reconstructed. We use  $z'_t = RNN(\mathbf{M}^\top w_t, h_t)$  to update the memory using normal memory access mechanisms, then redo the least-square attention.